

Financial Algebra Unit 3-6 Lesson Plan

Text: *Financial Algebra* by Robert Gerver and Richard Sgroi

Unit number and title: Unit 3-6 Continuous Compounding

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Short Description:

Compounding interest daily makes money grow more quickly than simple interest. This unit covers the functions that are used to increase a value toward infinity, which is the process of continuous compounding.

LESSON PLAN

TEACHER: Teacher Prep/ Lesson Plan

- **Essential Question**

How can interest be compounded continuously?

- **Lesson Objectives**

The student can:

1. Compute interest on an account that is continuously compounded.

- **Statement of pre-requisite skills needed**

Skills taught in:

Unit 3-3 Savings Accounts

Unit 3-4 Explore Compound Interest

Unit 3-5 Compound Interest Formula

- **New Vocabulary:**

| | |
|--------------------------------------|--|
| Limit | A concept in calculus which means an unreachable value. |
| Finite | Something that has an end and can be represented by a real number. |
| Infinite | Something without end, that cannot be represented by a real number. |
| Continuous Compounding | A method of calculating interest so that it is compounded on an infinite number of times each year rather than being compounded every minute, or even microsecond. |
| Exponential base (e) | The exponential base e is an irrational number which is a non-terminating, non-repeating decimal with an approximate value of $e \approx 2,718281828...$ |
| Continuous Compound Interest Formula | A formula for calculating continuous compound interest; $B = pe^{rt}$, where B is the ending balance, p is the principal, e is the exponential base, r is the interest rate, and t is the number of years the principal earns interest. |

- **State Standards addressed:**

Math: 1.1.4; 1.2; 2.2.2; 3.3.2

Algebra 1: A1.1.A; A1.1.D; A1.1.E; A1.2.F; A1.3.A; A1.3.B; A1.5.A; A1.5.B;
A1.5.C; A1.5.D; A1.7.C

Algebra 2: A2.1.A; A2.1.C; A2.2.A; A2.5.A; A2.8.A; A2.8.B; A2.8.C; A2.8.D;
A2.8.E; A2.8.F

Reading: 1.2.2; 2.1.4; 2.1.5; 2.3.4

Common Core Standards: Number and Quantity – The Real Number System N-
RN; Algebra – Seeing Structure in Expressions A-SSE

- **Set-up information (Remind students to follow these basic rules.)**

- Be Prepared to work
- No Teasing
- Proper Computer Usage

- **Teacher Assessment of student learning (scoring guide, rubric)**

Informal Assessments:

1. Walk around
2. Thumbs up or down
3. Homework

Formal Assessments:

1. End of Unit test

- **Summary of learning**

1. Introduce the vocabulary to the students.
 - a. Give the vocabulary list without definitions
 - b. Give the definitions to the vocabulary list
 - c. Discussion about each term of the vocabulary
2. Ask:
 - a. How can interest be compounded continuously?
 - b. Can there be compounding every half-second?
3. Work on Examples to Strengthen skills
 - a. Example 1, page 151
 - b. Example 2, page 151
 - c. Example 3, page 152
 - d. Example 4, page 152
 - e. Example 5, page 153
 - f. Example 6, page 153
4. Check for Understanding
 - a. Check Your Understanding 1, page 151
 - b. Check Your Understanding 2, page 151
 - c. Check Your Understanding 3, page 152
 - d. Check Your Understanding 4, page 152
 - e. Check your Understanding 5, page 153
 - f. Check your Understanding 6, page 153
5. Assess with Applications

REACHING ALL LEARNERS – Differentiated Instruction for students with

| Developing | On-level | Advanced |
|------------|----------|----------|
|------------|----------|----------|

| Knowledge | Knowledge | Knowledge |
|---|---|---|
| <input type="checkbox"/> Needs help working Example 1, page 151 (Group work) | <input type="checkbox"/> Able to work Example 1, page 151 without assistance | <input type="checkbox"/> Able to create additional problems like Example 1, page 151 |
| <input type="checkbox"/> Needs help working Example 2, page 151 (Group work) | <input type="checkbox"/> Able to work Example 2, page 151 without assistance | <input type="checkbox"/> Able to create additional problems like Example 2, page 151 |
| <input type="checkbox"/> Needs help working Example 3, page 152 (Group work) | <input type="checkbox"/> Able to work Example 3, page 152 without assistance | <input type="checkbox"/> Able to create additional problems like Example 3, page 152 |
| <input type="checkbox"/> Needs help working Example 4, page 152 (Group work) | <input type="checkbox"/> Able to work Example 4, page 152 without assistance | <input type="checkbox"/> Able to create additional problems like Example 4, page 152 |
| <input type="checkbox"/> Needs help working Example 5, page 153 (Group work) | <input type="checkbox"/> Able to work Example 5, page 153 without assistance | <input type="checkbox"/> Able to create additional problems like Example 4, page 153 |
| <input type="checkbox"/> Needs help working Example 6, page 153 (Group work) | <input type="checkbox"/> Able to work Example 6, page 153 without assistance | <input type="checkbox"/> Able to create additional problems like Example 4, page 153 |
| <input type="checkbox"/> | <input type="checkbox"/> Able to work the Check Your Understanding problems, pages 151-153 | <input type="checkbox"/> Able to work and explain the Check Your Understanding problems, pages 151-153 |
| <input type="checkbox"/> Exit Slip consisting of answering the question: How does today's class relate to me? | <input type="checkbox"/> Exit Slip consisting of answering the question: How does today's class relate to me? | <input type="checkbox"/> Exit Slip consisting of answering the question: How does today's class relate to me? |

- **Optional activities**

Hands-on Labs

- **Career Applications**

Banker

Venture Capitalist

Economist

Builder

Investor

Lawyer

Doctor

Teacher

Laborer

- **Evaluation of Lesson Plan**

What went well?

What did not go as well as planned?

What would I keep and what would I toss? Why?

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How well did the students master the skills? Will we need to review this in order for them to remember the information long-term?

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Unit 3-6 Continuous Compounding Quiz

Answer Key

Solution to #1.

Use the Continuous Compound Interest Formula.

$$B = pe^{rt}$$

Substitute

$$B = \$500(2.718281828)^{0.275(4)}$$

Calculate

$$\$2055.76$$

Definitions:

Finite: Something that has an end and can be represented by a real number

Continuous Compounding: A method of calculating interest so that it is compounded an infinite number of times each year rather than being compounded every minute, or every microsecond

Exponential Base: The exponential base e is an irrational number which is a non-terminating, non-repeating decimal with an approximate value of $e \approx 2.718281828$

Two Tools: Calculator, Computer

Unit 3-6 Continuous Compounding Quiz

Answer the following question on this paper. Show your work or explain your key strokes on the calculator as this will also be a part of the grade.

Formulas / Data:

Exponential base (e) \approx 2.718281828

Continuous Compound Interest Formula: $B = pe^{rt}$

Where B = Ending Balance

p = principal

e = exponential base

r = interest rate expressed as a decimal

t = number of years

1. You deposit \$500 at 2.75% interest, compounded continuously, what would be your ending balance to the nearest cent after four years?

Define the following terms:

2. Finite

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3. Continuous Compounding

4. Exponential Base

5. Name at least two tools that can be used to help with Continuous Compounding calculations?

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